

Algebra 1 Study Guide 6.1 - 6.3

Evaluate the expression. Be sure to rewrite any fractional exponents in radical form first.

1. $6.4^0 = 1$

2. $3^{-2} = \frac{1}{3^2} = \frac{1}{9}$

3. $81^{\frac{1}{4}} = \sqrt[4]{81} = 3$

Evaluate the expression. Be sure to rewrite any expression that is in exponent form, in radical form first.

4. $\left(\frac{1}{64}\right)^{1/3} = \sqrt[3]{\frac{1}{64}} = \frac{1}{4}$

5. $1000^{2/3} = \left(\sqrt[3]{1000}\right)^2 = (10)^2 = 100$

6. $(\sqrt{36})^3 = (6)^3 = 216$

7. $(8)^{-2/3} = \frac{1}{8^{2/3}} = \left(\frac{1}{\sqrt[3]{8}}\right)^2 = \frac{1}{2^2} = \frac{1}{4}$

Simplify the expression. Write your answer using only positive exponents. You must show work for this!

8. $\left(\frac{3d^2}{4}\right)^{-5} = \frac{3^{-5}d^{-10}}{4^{-5}} = \frac{4^5}{3^5d^{10}} = \frac{1024}{243d^{10}}$

$$9. (4d^8)^{-5} = 4^{-5} d^{-40} = \frac{1}{4^5 d^{40}} = \frac{1}{1024d^{40}}$$

$$10. -7r^{-9}s^0 = \frac{7 \cdot 1}{r^9} = \frac{7}{r^9}$$

$$11. \frac{3^0 x^{-7} z^0}{4^2 y^{-3}} = \frac{1 \cdot 1 \cdot y^3}{x^7 \cdot 4^2} = \frac{y^3}{16x^7}$$

$$12. (x^6)^3 = x^{18}$$

Simplify the expression. Write your answer using only positive exponents.

$$13. \left(\frac{2x^{-4}}{12x^{-3}y^0} \right)^3 = \left(\frac{2}{12} \cdot \frac{x^3}{x^4} \cdot \frac{1}{y^0} \right)^3 = \left(\frac{1}{6} \cdot \frac{1}{x^1} \cdot \frac{1}{1} \right)^3$$

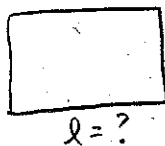
$$= \left(\frac{1}{6x} \right)^3 = \frac{1}{6^3 x^3} = \frac{1}{216x^3}$$

Find the indicated real n th root(s) of a .

$$14. n=4, a=81 \quad \sqrt[4]{81} = 3$$

$$15. n=4, a=-625 \quad \sqrt[4]{-625} = \text{no real solution}$$

16. The area of a rectangular yard with a width of $7a^3b$ feet is $9a^2b^5$ square feet. What is the length?



$$w = 7a^3b$$

$$l = ?$$

$$A = lw$$

$$A = 9a^2b^5$$

$$9a^2b^5 = l \cdot (7a^3b)$$

$$\frac{9a^2b^5}{7a^3b} = l$$

$$\frac{9b^4}{7a} = l$$

The length is $\frac{9b^4}{7a}$ feet.

17. A galaxy is 10^5 light-years away from Earth. Another galaxy is 10^7 times farther away from Earth than the first galaxy. How far away (in light-years) is the second galaxy? Write your answer in scientific notation and in standard form.

$$10^5 \cdot 10^7 = 10^{12}$$

scientific 1×10^{12}
standard 1000000000000

The second galaxy is 1×10^{12} light years away from Earth.

Determine whether the table represents a *linear* or an *exponential* function. Explain and be sure to show proof of your conclusion.

18. x's ↑ by 1

x	y
0	2
1	4
2	6
3	8

$$\frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{8 - 6}{1 - 0} = 2$$

$$\frac{6 - 4}{2 - 1} = 2$$

$$\frac{4 - 2}{3 - 2} = 2$$

} constant difference
↓
would be "m" slope

The table represents a linear function because the difference of consecutive y's is constant.

19. x's ↑ by 1

x	y
1	5
2	10
3	20
4	40

$$\frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{10 - 5}{2 - 1} = 5$$

$$\frac{20 - 10}{3 - 2} = 10$$

} Not constant,
not linear

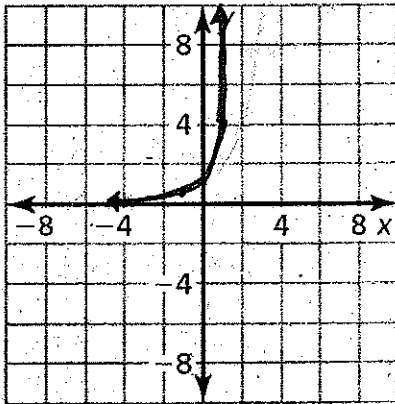
$$\frac{y_2}{y_1} = \frac{10}{5} = 2$$

$$\frac{20}{10} = 2$$

$$\frac{40}{20} = 2$$

} The table represents an exponential function because the ratio of consecutive y's is constant.
base = 2

20. Graph $y = 4^x$. Be sure to show an x and y table. Describe the domain and range.



$$y = 4^x$$

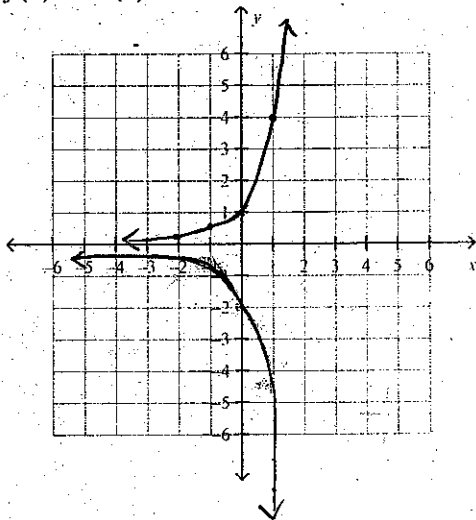
x	y
-1	$\frac{1}{4}$
0	1
1	4
2	16

D: \mathbb{R} (the set of all real numbers)

R: $\{y > 0\}$

Graph the function. Compare the function to the graph of the parent function. Describe the domain and range of f .

21. $f(x) = -2(4)^x$



parent

$$y = 4^x$$

x	y
-1	$\frac{1}{4}$
0	1
1	4

$$f(x) = -2(4)^x$$

x	f(x)
-1	$-\frac{1}{2}$
0	-2
1	-8

D: \mathbb{R}

R: $\{y < 0\}$

$f(x) = -2(4)^x$ is a reflection over the x-axis and a vertical stretch by a factor of 2 of $y = 4^x$.