

5.5**Notetaking with Vocabulary****Core Concepts****Solving Linear Equations by Graphing**

Step 1 To solve the equation $ax + b = cx + d$, write two linear equations.

$$y = ax + b \quad \text{and} \quad y = cx + d$$

$$\begin{array}{l} y = ax + b \\ y = cx + d \end{array} \quad \left. \begin{array}{l} \text{now a} \\ \text{System} \end{array} \right\}$$

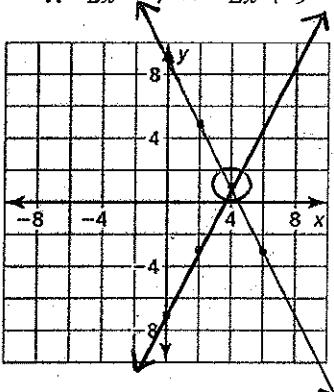
Step 2 Graph the system of linear equations. The x -value of the solution of the system of linear equations is the solution of the equation $ax + b = cx + d$.

(x, y)
 $X =$

Practice:

In Exercises 1–9, solve the equation by graphing. Check your solution(s).

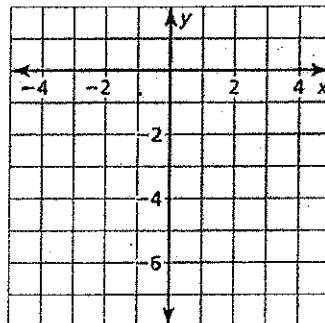
1. $2x - 7 = -2x + 9$



$$y = 2x - 7$$

$$y = -2x + 9$$

2. $3x = x - 4$



(4, 1)

$X = 4$

Check:

$$\begin{aligned} 2(4) - 7 &= -2(4) + 9 \\ 8 - 7 &= -8 + 9 \\ 1 &= 1 \checkmark \end{aligned}$$

Algebraically...

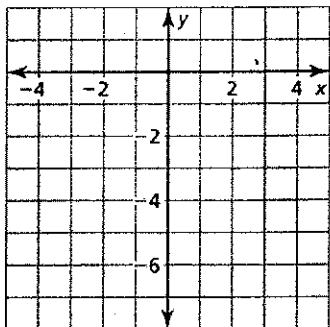
$$\begin{array}{rcl} 2x - 7 & = & -2x + 9 \\ +2x & & +2x \end{array}$$

$$4x - 7 = 9$$

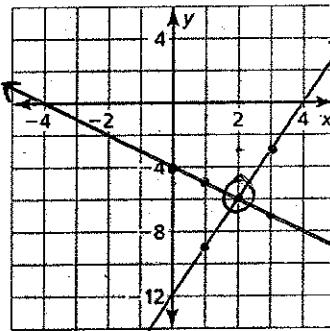
$$\frac{4x}{4} = \frac{16}{4}$$

$X = 4$

$$3. \quad 4x + 1 = -2x - 5$$



$$4. \quad -x - 4 = 3(x - 4)$$



$$-x - 4 = 3x - 12$$

$$y = -x - 4$$

$$y = 3x - 12$$

$$(2, -6)$$

$$x = 2$$

$$-(2) - 4 = 3(2 - 4)$$

$$-6 = 3(-2)$$

$$-6 = -6 \checkmark$$

Solving Absolute Value Equations by Graphing

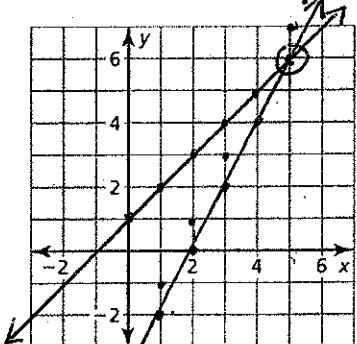
How many solutions are possible with absolute value equations? $\begin{matrix} 2 \text{ solutions} \\ (2, 1 \text{ or } 0) \end{matrix}$

Recall that an absolute value equation of the form $|ax + b| = |cx + d|$ has two related equations.

$$\begin{aligned} ax + b &= cx + d & \text{or} & \quad ax + b = -(cx + d) \\ ax + b &= -cx - d \end{aligned}$$

Solve $|x + 1| = |2x - 4|$ by graphing. Check your solutions.

(Apply the steps for solving an equation by graphing to each of the related equations.)



$$(5, 6)$$

$$x = 5$$

$$x + 1 = 2x - 4$$

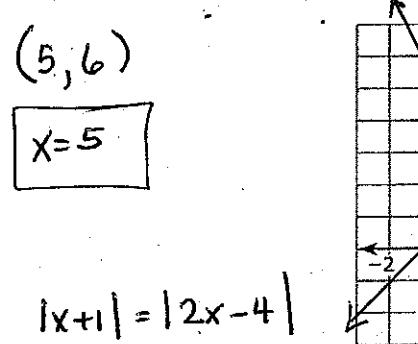
$$y = x + 1$$

$$y = 2x - 4$$

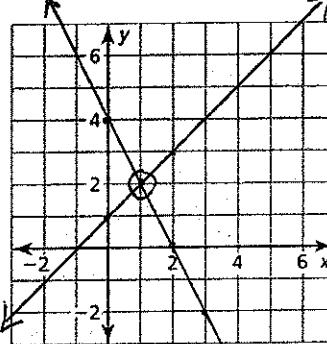
$$\text{Check: } |5+1| = |2(5)-4|$$

$$|6| = |6|$$

$$6 = 6 \checkmark$$



$$|x+1| = |2x-4|$$



$$x + 1 = -2x + 4$$

$$y = x + 1$$

$$y = -2x + 4$$

$$(1, 2)$$

$$x = 1$$

Check.

$$|1+1| = |2(1)-4|$$

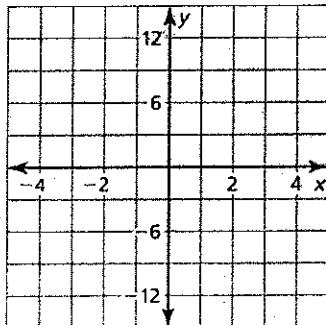
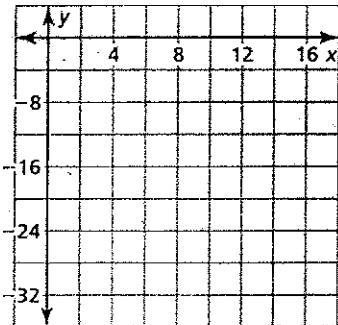
$$|2| = |-2|$$

$$2 = 2 \checkmark$$

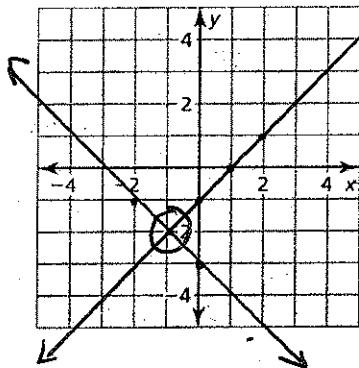
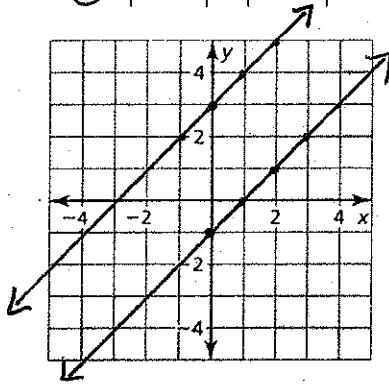
Two solutions! $x = 1$
 $x = 5$

5.5 Notetaking with Vocabulary (continued)

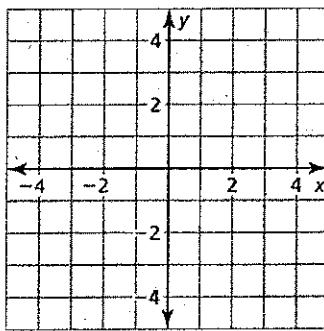
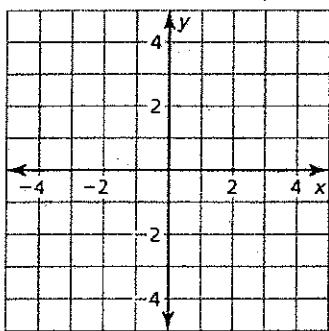
5. $|3x| = |2x + 10|$



6. $|x - 1| = |x + 3|$



7. $|x + 4| = |2 - x|$



$$x - 1 = x + 3 \quad \text{or} \quad x - 1 = -x - 3$$

$$-(x + 3)$$

$$y = x - 1$$

$$y = x + 3$$

No solution

$$y = x - 1$$

$$y = -x - 3$$

(-1, -2)

$$x = -1$$

One solution

$$|-1 - 1| = |-1 + 3|$$

$$|-2| = |2|$$

$$2 = 2$$