

2.6

Notetaking with Vocabulary

Learning target: Understand solving liner inequalities.

Success criteria: I can solve absolute value inequalities.

Write the meaning of each vocabulary term.

absolute value inequality - an inequality that contains an absolute value expression.

absolute deviation - used in modeling - the absolute value of the ^{ideal/axis.} difference of x and a given value.

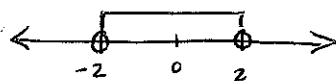
already did this

error distance

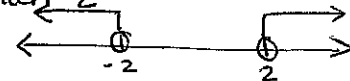
Notes: $|x| < 2$ the graph means the distance b/w x and 0 is less than 2

$|x| = 2$ means the distance b/w x and 0 is 2.

$|x| > 2$ means the distance between x and 0 is greater than 2



$x > -2$ and $x < 2$
looks like an "and"



looks like an "or"

the graph of this is the graph of $x < -2$ or $x > 2$

Core Concepts

Solving Absolute Value Inequalities

To solve $|ax + b| < c$ for $c > 0$, solve the compound inequality

$ax + b > -c$ and $ax + b < c$.
less than is and

To solve $|ax + b| > c$ for $c > 0$, solve the compound inequality

$ax + b < -c$ or $ax + b > c$.
great "or" than is or

In the inequalities above, you can replace $<$ with \leq and $>$ with \geq .

Notes:

2.6 Notetaking with Vocabulary (continued)

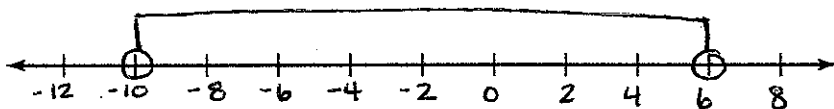
Practice

In Exercises 1–9, solve the inequality. Graph the solution, if possible.

1. $|y+2| < 8$ (distance less than 8 → and)

$$\begin{array}{r} y+2 < 8 & \text{and} & y+2 > -8 \\ -2 & -2 & -2 & -2 \end{array}$$

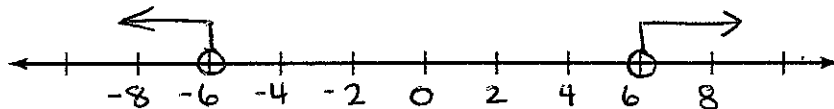
$$y < 6 \text{ and } y > -10$$



2. $|\frac{q}{3}| > 2$ (distance greater than 2 → or)

$$\frac{q}{3} > 2 \text{ or } \frac{q}{3} < -2$$

$$q > 6 \text{ or } q < -6$$



3. $3|2a+5|+10 \leq 37$

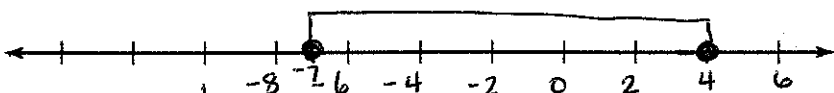
$$\frac{3|2a+5|}{3} \leq \frac{27}{3}$$

$$|2a+5| \leq 9 \text{ distance less than 9 "and"}$$

$$\begin{array}{r} 2a+5 \leq 9 & \text{and} & 2a+5 \geq -9 \\ -5 & -5 & -5 & -5 \end{array}$$

$$\frac{2a}{2} \leq \frac{4}{2} \qquad \frac{2a}{2} \geq \frac{-14}{2}$$

$$a \leq 4 \text{ and } a \geq -7$$

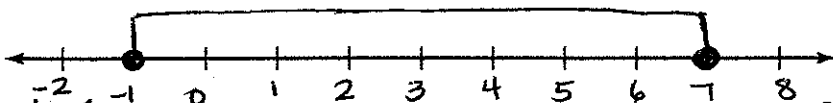


4. $|y-3| \leq 4$

less than 4

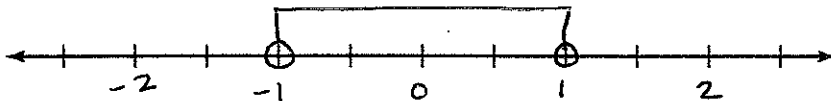
$$\begin{array}{r} y-3 \leq 4 & \text{and} & y-3 \geq -4 \\ +3 & +3 & +3 & +3 \end{array}$$

$$y \leq 7 \text{ and } y \geq -1$$



2.6 Notetaking with Vocabulary (continued)

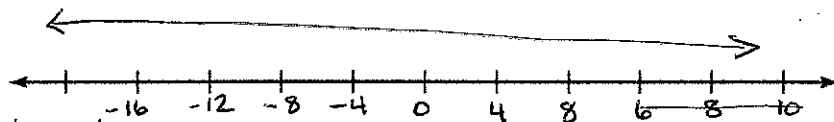
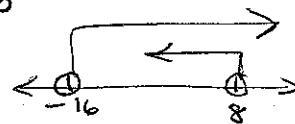
5. $|3+r|-4 < 0$
 $\begin{matrix} +4 & +4 \\ |3+r| < 4 \end{matrix}$
 and
 $3+r < 4$ and $3+r > -4$
 $r < 1$ and $r > -1$



6. $|f+12| > -4$
 $f+12 > -4$ or $f+12 < +4$
 $f > -16$ or $f < 8$

can just look - won't be \geq zero so they know above is true.

All real numbers are solutions.

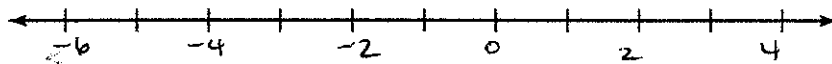
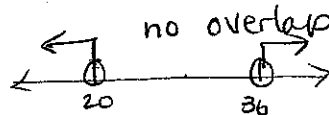


7. $|\frac{x}{4}-7| < -2$ also - look \rightarrow Is this possible?

$\frac{x}{4}-7 < -2$ and $\frac{x}{4}-7 > 2$

$\frac{x}{4} < 5$ and $\frac{x}{4} > 9$

$x < 20$ and $x > 36$
 No solution



8. $|4x-7|+8 \geq 17$
 $\begin{matrix} -8 & -8 \\ |4x-7| \geq 9 \end{matrix}$

$4x-7 \geq 9$

or $4x-7 \leq -9$

$4x \geq 16$

$4x \leq -2$

$x \geq 4$

$x \leq -\frac{1}{2}$

$x \leq -\frac{1}{2}$

$$9. \frac{6|3-k|+14}{-14} > \frac{14}{-14}$$

$$\frac{3-k}{-3} > 0 \quad \text{or} \quad \frac{3-k}{-3} < 0$$

$$\frac{6|3-k|}{6} > \frac{0}{6}$$

$$\frac{-k}{-1} > \frac{-3}{-1} \quad \text{or} \quad \frac{-k}{-1} < \frac{-3}{-1}$$

$$|3-k| > 0$$

$$k < 3 \quad \text{or} \quad k > 3$$



10. At a certain company, the average starting salary s for a new worker is $\$25,000$. The actual salary has an absolute deviation of at most $\$1800$. Write and solve an inequality to find the range of the starting salaries.

equation - ok

$$\text{ab. dev} = |x - \text{given value}|$$

$$1800 = |x - 25,000|$$

$$\begin{array}{r} x - 25,000 = 1800 \\ +25,000 \quad +25,000 \\ \hline \end{array}$$

$$x = 26,800$$

$$\begin{array}{r} x - 25,000 = -1800 \\ +25,000 \quad +25,000 \\ \hline \end{array}$$

$$x = 23,200$$

Starting salaries range from
 $\$23,200$ to $\$26,800$.